## Curriculum Framework Cambridge Lower Secondary Mathematics 1112



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## Introduction

Welcome to the Cambridge Lower Secondary Mathematics Curriculum Framework.
This framework provides a comprehensive set of progressive learning objectives for mathematics. The objectives detail what the learner should know or what they should be able to do in each year of lower secondary education. The learning objectives provide a structure for teaching and learning and a reference against which learners' ability and understanding can be checked.

The Cambridge Lower Secondary mathematics curriculum is presented in six content areas: Number, Algebra, Geometry, Measure, Handling data and Problem solving. The first five content areas are all underpinned by Problem solving, which provides a structure for the application of mathematical skills. Mental strategies are also a key part of the Number content. Together, these two areas form a progressive step preparing students for entry onto IGCSE ${ }^{\circledR}$ level courses. This curriculum focuses on principles, patterns, systems, functions and relationships so that learners can apply their mathematical knowledge and develop a holistic understanding of the subject. The Cambridge Lower Secondary Mathematics curriculum framework continues the journey from the Cambridge Primary mathematics framework and provides a solid foundation upon which the later stages of education can be built.

The Cambridge Curriculum is founded on the values of the University of Cambridge and best practice in schools. The curriculum is dedicated to developing learners who are confident, responsible, innovative and engaged. Each curriculum framework for English, mathematics and science is designed to engage learners in an active and creative learning journey.

## Note on codes

Each learning objective has a unique curriculum framework code, e.g. 7Ni1. These codes appear in the Cambridge International Teacher Guide, schemes of work and other published resources. Each sub-strand has a green reporting code, e.g. Ni. These codes appear in Checkpoint feedback reports. Problem solving is not assessed separately and so does not have a reporting code.

## Stage 7

## Number

## Ni Integers, powers and roots

- 7Ni1 Recognise negative numbers as positions on a number line, and order, add and subtract positive and negative integers in context
- 7Ni2 Recognise multiples, factors, common factors, primes (all less than 100), making use of simple tests of divisibility; find the lowest common multiple in simple cases; use the 'sieve' for generating primes developed by Eratosthenes
- 7 Ni 3 Recognise squares of whole numbers to at least $20 \times 20$ and the corresponding square roots; use the notation $7^{2}$ and $\sqrt{49}$


## Np Place value, ordering and rounding

- $\mathbf{7 N p} 1$ Interpret decimal notation and place value; multiply and divide whole numbers and decimals by 10, 100 or 1000
- 7Np2 Order decimals including measurements, changing these to the same units
- 7 Np 3 Round whole numbers to the nearest 10,100 or 1000 and decimals, including measurements, to the nearest whole number or one decimal place


## Nf Fractions, decimals, percentages, ratio and proportion

- 7Nf1 Recognise the equivalence of simple fractions, decimals and percentages
- 7Nf2 Simplify fractions by cancelling common factors and identify equivalent fractions; change an improper fraction to a mixed number, and vice versa; convert terminating decimals to fractions, e.g. $0.23=\frac{23}{100}$
- 7Nf3 Compare two fractions by using diagrams, or by using a calculator to convert the fractions to decimals, e.g. $\frac{3}{5}$ and $\frac{13}{20}$
- 7Nf4 Add and subtract two simple fractions, e.g. $\frac{1}{8}+\frac{9}{8}, \frac{11}{12}-\frac{5}{6}$; find fractions of quantities (whole number answers); multiply a fraction by an integer
- 7Nf5 Understand percentage as the number of parts in every 100; use fractions and percentages to describe parts of shapes, quantities and measures
- 7Nf6 Calculate simple percentages of quantities (whole number answers) and express a smaller quantity as a fraction or percentage of a larger one
- 7Nf7 Use percentages to represent and compare different quantities
- 7Nf8 Use ratio notation, simplify ratios and divide a quantity into two parts in a given ratio
- 7Nf9 Recognise the relationship between ratio and proportion
- 7Nf10 Use direct proportion in context; solve simple problems involving ratio and direct proportion


## Nc Calculation

## Mental strategies

- $\mathbf{7 N c} 1$ Consolidate the rapid recall of number facts, including positive integer complements to 100, multiplication facts to $10 \times 10$ and associated division facts
- 7Nc2 Use known facts and place value to multiply and divide two-digit numbers by a single-digit number, e.g. $45 \times 6,96 \div 6$
- 7Nc3 Know and apply tests of divisibility by 2, 3, 5, 6, 8, 9, 10 and 100
- 7Nc4 Use known facts and place value to multiply simple decimals by one-digit numbers, e.g. $0.8 \times 6$
- 7Nc5 Calculate simple fractions and percentages of quantities, e.g. one quarter of $64,20 \%$ of 50 kg
- 7Nc6 Use the laws of arithmetic and inverse operations to simplify calculations with whole numbers and decimals
- 7Nc7 Use the order of operations, including brackets, to work out simple calculations


## Addition and subtraction

- 7Nc8 Add and subtract integers and decimals, including numbers with different numbers of decimal places


## Multiplication and division

- 7Nc9 Multiply and divide decimals with one and/or two places by single-digit numbers, e.g. $13.7 \times 8,4.35 \div 5$
- 7 Nc 10 Know that in any division where the dividend is not a multiple of the divisor there will be a remainder, e.g. $157 \div 25=6$ remainder 7 . The remainder can be expressed as a fraction of the divisor, e.g. $157 \div 25=6 \frac{7}{25}$
- 7Nc11 Know when to round up or down after division when the context requires a whole-number answer


## Algebra

## Ae Expressions, equations and formulae

- 7Ae1 Use letters to represent unknown numbers or variables; know the meanings of the words term, expression and equation
- 7Ae2 Know that algebraic operations follow the same order as arithmetic operations
- 7Ae3 Construct simple algebraic expressions by using letters to represent numbers
- 7Ae4 Simplify linear expressions, e.g. collect like terms; multiply a constant over a bracket
- 7Ae5 Derive and use simple formulae, e.g. to change hours to minutes
- 7Ae6 Substitute positive integers into simple linear expressions/formulae
- 7Ae7 Construct and solve simple linear equations with integer coefficients (unknown on one side only), e.g. $2 x=8,3 x+5=14,9-2 x=7$


## As Sequences, functions and graphs

- 7As1 Generate terms of an integer sequence and find a term given its position in the sequence; find simple term-to-term rules
- 7As2 Generate sequences from spatial patterns and describe the general term in simple cases
- 7As3 Represent simple functions using words, symbols and mappings
- 7As4 Generate coordinate pairs that satisfy a linear equation, where $y$ is given explicitly in terms of $x$; plot the corresponding graphs; recognise straight-line graphs parallel to the $x$ - or $y$-axis


## Geometry

## Gs Shapes and geometric reasoning

- 7Gs1 Identify, describe, visualise and draw 2D shapes in different orientations
- 7Gs2 Use the notation and labelling conventions for points, lines, angles and shapes
- 7Gs3 Name and identify side, angle and symmetry properties of special quadrilaterals and triangles, and regular polygons with 5,6 and 8 sides
- 7Gs4 Estimate the size of acute, obtuse and reflex angles to the nearest $10^{\circ}$
- 7Gs5 Start to recognise the angular connections between parallel lines, perpendicular lines and transversals
- 7Gs6 Calculate the sum of angles at a point, on a straight line and in a triangle, and prove that vertically opposite angles are equal; derive and use the property that the angle sum of a quadrilateral is $360^{\circ}$
- 7Gs7 Solve simple geometrical problems by using side and angle properties to identify equal lengths or calculate unknown angles, and explain reasoning
- 7Gs8 Recognise and describe common solids and some of their properties, e.g. the number of faces, edges and vertices
- 7Gs9 Recognise line and rotation symmetry in 2D shapes and patterns; draw lines of symmetry and complete patterns with two lines of symmetry; identify the order of rotation symmetry
- 7Gs10 Use a ruler, set square and protractor to:
- measure and draw straight lines to the nearest millimetre
- measure and draw acute, obtuse and reflex angles to the nearest degree
- draw parallel and perpendicular lines
- construct a triangle given two sides and the included angle (SAS) or two angles and the included side (ASA)
- construct squares and rectangles
- construct regular polygons, given a side and the internal angle


## Gp Position and movement

- 7Gp1 Read and plot coordinates of points determined by geometric information in all four quadrants
- 7Gp2 Transform 2D points and shapes by:
- reflection in a given line
- rotation about a given point
- translation

Know that shapes remain congruent after these transformations

## Measure

## Gl Length, mass and capacity

7GI1 - 7Ml1 Choose suitable units of measurement to estimate, measure, calculate and solve problems in everyday contexts

7Gl2 - 7Ml2 Know abbreviations for and relationships between metric units; convert between:

- kilometres (km), metres (m), centimetres (cm), millimetres (mm)
- tonnes ( t ), kilograms ( kg ) and grams ( g )
- litres (l) and millilitres (ml)

7GI3 - 7MI3 Read the scales on a range of analogue and digital measuring instruments

## Gt Time and rates of change

7Gt1 • 7Mt1 Draw and interpret graphs in real life contexts involving more than one stage, e.g. travel graphs

7Gt2

- 7Mt2 Know the relationships between units of time; understand and use the 12-hour and 24-hour clock systems; interpret timetables; calculate time intervals

Ga Area, perimeter and volume
7Ga1 - 7Ma1 Know the abbreviations for and relationships between square metres $\left(\mathrm{m}^{2}\right)$, square centimetres $\left(\mathrm{cm}^{2}\right)$, square millimetres $\left(\mathrm{mm}^{2}\right)$
7 Ga 2 - 7Ma2 Derive and use formulae for the area and perimeter of a rectangle; calculate the perimeter and area of compound shapes made from rectangles
7Ga3 - 7Ma3 Derive and use the formula for the volume of a cuboid; calculate volumes of cuboids
7Ga4 - 7Ma4 Calculate the surface area of cubes and cuboids from their nets

## Handling data

Dc Planning and collecting data

- 7Dc1 Decide which data would be relevant to an enquiry and collect and organise the data
- 7Dc2 Design and use a data collection sheet or questionnaire for a simple survey
- 7Dc3 Construct and use frequency tables to gather discrete data, grouped where appropriate in equal class intervals


## Dp Processing and presenting data

- 7Dp1 Find the mode (or modal class for grouped data), median and range
- 7Dp2 Calculate the mean, including from a simple frequency table
- 7Dp3 Draw and interpret:
- bar-line graphs and bar charts
- frequency diagrams for grouped discrete data
- simple pie charts
- pictograms


## Di Interpreting and discussing results

- 7Di1 Draw conclusions based on the shape of graphs and simple statistics
- 7Di2 Compare two simple distributions using the range and the mode, median or mean


## Db Probability

- 7Db1 Use the language of probability to describe and interpret results involving likelihood and chance
- 7Db2 Understand and use the probability scale from 0 to 1
- 7Db3 Find probabilities based on equally likely outcomes in simple contexts
- 7Db4 Identify all the possible mutually exclusive outcomes of a single event
- 7Db5 Use experimental data to estimate probabilities
- 7Db6 Compare experimental and theoretical probabilities in simple contexts


## Problem solving

## Using techniques and skills in solving mathematical problems

- 7Pt1 Use the laws of arithmetic and inverse operations to simplify calculations with whole numbers and decimals
- 7Pt2 Manipulate numbers, algebraic expressions and equations, and apply routine algorithms
- 7Pt3 Understand everyday systems of measurement and use them to estimate, measure and calculate
- 7Pt4 Recognise and use spatial relationships in two and three dimensions
- 7Pt5 Draw accurate mathematical diagrams, graphs and constructions
- 7Pt6 Check results of calculations by using inverse operations
- 7Pt7 Estimate, approximate and check their working
- 7Pt8 Solve word problems involving whole numbers, percentages, decimals, money or measures: choose operations and mental or written methods appropriate to the numbers and context, including problems with more than one step


## Using understanding and strategies in solving problems

- 7Ps1 Identify and represent information or unknown numbers in problems, making correct use of numbers, symbols, words, diagrams, tables and graphs
- 7Ps2 Recognise mathematical properties, patterns and relationships, generalising in simple cases
- 7Ps3 Work logically and draw simple conclusions
- 7Ps4 Relate results or findings to the original context and check that they are reasonable
- 7Ps5 Record and explain methods, results and conclusions
- 7Ps6 Discuss and communicate findings effectively, orally and in writing


## Stage 8

## Number

## Ni Integers, powers and roots

- $\mathbf{8 N i 1}$ Add, subtract, multiply and divide integers
- $\mathbf{8 N i 2}$ Identify and use multiples, factors, common factors, highest common factors, lowest common multiples and primes; write a number in terms of its prime factors, e.g. $500=2^{2} \times 5^{3}$
- 8 Ni 3 Calculate squares, positive and negative square roots, cubes and cube roots; use the notation $\sqrt{49}$ and $\sqrt[3]{64}$ and index notation for positive integer powers

Np Place value, ordering and rounding

- $\quad \mathbf{8 N p} 1$ Read and write positive integer powers of 10; multiply and divide integers and decimals by $0.1,0.01$
- 8Np2 Order decimals, including measurements, making use of the $=, \neq,>$ and $<$ signs
- $\mathbf{8 N p} 3$ Round whole numbers to a positive integer power of 10, e.g. 10, 100, 1000 or decimals to the nearest whole number or one or two decimal places


## Nf Fractions, decimals, percentages, ratio and proportion

- 8Nf1 Find equivalent fractions, decimals and percentages by converting between them
- 8Nf2 Convert a fraction to a decimal using division; know that a recurring decimal is a fraction
- 8Nf3 Order fractions by writing with common denominators or dividing and converting to decimals
- $\mathbf{8 N f 4}$ Add and subtract fractions and mixed numbers; calculate fractions of quantities (fraction answers); multiply and divide an integer by a fraction
- 8Nf5 Calculate and solve problems involving percentages of quantities and percentage increases or decreases; express one given number as a fraction or percentage of another
- 8Nf6 Use equivalent fractions, decimals and percentages to compare different quantities
- $\mathbf{8 N f 7}$ Simplify ratios, including those expressed in different units; divide a quantity into more than two parts in a given ratio
- $\mathbf{8 N f} \mathbf{8}$ Use the unitary method to solve simple problems involving ratio and direct proportion


## Nc Calculation

## Mental strategies

- $8 N c 1$ Use known facts to derive new facts, e.g. given $20 \times 38=760$, work out $21 \times 38$
- $\mathbf{8 N c 2}$ Recall squares to $20 \times 20$, cubes to $5 \times 5 \times 5$, and corresponding roots
- 8Nc3 Recall simple equivalent fractions, decimals and percentages
- $\mathbf{8 N c} 4$ Use known facts and place value to multiply and divide simple fractions
- $\mathbf{8 N c 5}$ Use known facts and place value to multiply and divide simple decimals, e.g. $0.07 \times 9,2.4 \div 3$
- $\mathbf{8 N c 6}$ Use known facts and place value to calculate simple fractions and percentages of quantities
- $\mathbf{8 N c}$ Recall relationships between units of measurement
- $\mathbf{8 N c 8}$ Solve simple word problems including direct proportion problems
- 8Nc9 Use the laws of arithmetic and inverse operations to simplify calculations with integers and fractions
- $\mathbf{8 N c} 10$ Use the order of operations, including brackets, with more complex calculations


## Addition and subtraction

- $\mathbf{8 N c} 11$ Consolidate adding and subtracting integers and decimals, including numbers with differing numbers of decimal places


## Multiplication and division

- $\mathbf{8 N c} 12$ Divide integers and decimals by a single-digit number, continuing the division to a specified number of decimal places, e.g. $68 \div 7$
- 8Nc13 Multiply and divide integers and decimals by decimals such as 0.6 or 0.06 , understanding where to place the decimal point by considering equivalent calculations, e.g. $4.37 \times 0.3=(4.37 \times 3) \div 10$, $92.4 \div 0.06=(92.4 \times 100) \div 6$


## Algebra

## Ae Expressions, equations and formulae

- 8Ae1 Know that letters play different roles in equations, formulae and functions; know the meanings of formula and function
- 8Ae2 Know that algebraic operations, including brackets, follow the same order as arithmetic operations; use index notation for small positive integer powers
- 8Ae3 Construct linear expressions
- 8Ae4 Simplify or transform linear expressions with integer coefficients; collect like terms; multiply a single term over a bracket
- 8Ae5 Derive and use simple formulae, e.g. to convert degrees Celsius $\left({ }^{\circ} \mathrm{C}\right)$ to degrees Fahrenheit ( ${ }^{\circ} \mathrm{F}$ )
- 8Ae6 Substitute positive and negative integers into formulae, linear expressions and expressions involving small powers, e.g. $3 x^{2}+4$ or $2 x^{3}$, including examples that lead to an equation to solve
- 8Ae7 Construct and solve linear equations with integer coefficients (unknown on either or both sides, without or with brackets)


## As Sequences, functions and graphs

- 8As1 Generate terms of a linear sequence using term-to-term and position-to-term rules; find term-to-term and position-to-term rules of sequences, including spatial patterns
- 8As2 Use a linear expression to describe the $n$th term of a simple arithmetic sequence, justifying its form by referring to the activity or practical context from which it was generated
- 8As3 Express simple functions algebraically and represent them in mappings
- 8As4 Construct tables of values and use all four quadrants to plot the graphs of linear functions, where $y$ is given explicitly in terms of $x$; recognise that equations of the form $y=m x+c$ correspond to straight-line graphs


## Geometry

## Gs Shapes and geometric reasoning

- 8Gs1 Know that if two 2D shapes are congruent, corresponding sides and angles are equal
- 8Gs2 Classify quadrilaterals according to their properties, including diagonal properties
- 8Gs3 Know that the longest side of a right-angled triangle is called the hypotenuse
- 8Gs4 Identify alternate angles and corresponding angles
- 8Gs5 Understand a proof that:
- the angle sum of a triangle is $180^{\circ}$ and that of a quadrilateral is $360^{\circ}$
- the exterior angle of a triangle is equal to the sum of the two interior opposite angles
- 8Gs6 Solve geometrical problems using properties of angles, of parallel and intersecting lines, and of triangles and special quadrilaterals, explaining reasoning with diagrams and text
- 8Gs7 Draw simple nets of solids, e.g. cuboid, regular tetrahedron, square-based pyramid, triangular prism
- 8Gs8 Identify all the symmetries of 2D shapes
- 8Gs9 Use a straight edge and compasses to construct:
- the midpoint and perpendicular bisector of a line segment
- the bisector of an angle
- 8Gs10 Use a ruler and compasses to construct:
- circles and arcs
- a triangle, given three sides (SSS)
- a triangle, given a right angle, hypotenuse and one side (RHS)


## Gp Position and movement

- 8 Gp 1 Find the midpoint of the line segment $A B$, given the coordinates of points $A$ and $B$
- 8Gp2 Transform 2D shapes by rotation, reflection and translation, and simple combinations of these transformations
- $\mathbf{8 G p 3}$ Understand and use the language and notation associated with enlargement; enlarge 2D shapes, given a centre of enlargement and a positive integer scale factor
- 8Gp4 Interpret and make simple scale drawings


## Measure

Gl Length, mass and capacity
8GI1 - 8M11 Choose suitable units of measurement to estimate, measure, calculate and solve problems in a range of contexts, including units of mass, length, area, volume or capacity
8GI2 - 8MI2 Know that distances in the USA, the UK and some other countries are measured in miles, and that one kilometre is about $\frac{5}{8}$ of a mile

## Gt Time and rates of change

8Gt1 - 8Mt1 Draw and interpret graphs in real life contexts involving more than one component, e.g. travel graphs with more than one person

## Ga Area, perimeter and volume

8Ga1 - 8Ma1 Know the definition of a circle and the names of its parts; know and use formulae for the circumference and area of a circle

- $\mathbf{8 M a} 2$ Derive and use formulae for the area of a triangle, parallelogram and trapezium; calculate areas of compound 2D shapes, and lengths, surface areas and volumes of cuboids
8Ga3 - 8Ma3 Use simple nets of solids to work out their surface areas


## Handling data

## Dc Planning and collecting data

- 8Dc1 Identify and collect data to answer a question; select the method of collection, sample size and degree of accuracy needed for measurements
- 8Dc2 Know the difference between discrete and continuous data
- 8Dc3 Construct and use:
- frequency tables with given equal class intervals to gather continuous data
- two-way tables to record discrete data


## Dp Processing and presenting data

- 8Dp1 Calculate statistics for sets of discrete and continuous data; recognise when to use the range, mean, median and mode and, for grouped data, the modal class
- 8Dp2 Draw, and interpret:
- frequency diagrams for discrete and continuous data
- pie charts
- simple line graphs for time series
- stem-and-leaf diagrams

Di Interpreting and discussing results

- 8Di1 Interpret tables, graphs and diagrams for discrete and continuous data, and draw conclusions, relating statistics and findings to the original question
- 8Di2 Compare two distributions, using the range and one or more of the mode, median and mean
- 8Di3 Compare proportions in two pie charts that represent different totals


## Db Probability

- 8Db1 Know that if the probability of an event occurring is $p$, then the probability of it not occurring is $1-p$
- 8Db2 Find probabilities based on equally likely outcomes in practical contexts
- 8Db3 Find and list systematically all possible mutually exclusive outcomes for single events and for two successive events
- 8Db4 Compare estimated experimental probabilities with theoretical probabilities, recognising that:
- when experiments are repeated different outcomes may result
- increasing the number of times an experiment is repeated generally leads to better estimates of probability


## Problem solving

## Using techniques and skills in solving mathematical problems

- 8Pt1 Calculate accurately, choosing operations and mental or written methods appropriate to the numbers and context
- $\mathbf{8 P t} \mathbf{2}$ Use the order of operations, including brackets, with more complex calculations
- 8Pt3 Manipulate numbers, algebraic expressions and equations, and apply routine algorithms
- 8Pt4 Understand everyday measurement systems, using them to estimate, measure and calculate
- 8Pt5 Recognise and use spatial relationships in two and three dimensions
- 8Pt6 Draw accurate mathematical diagrams, graphs and constructions
- 8Pt7 Estimate, approximate and check working
- 8Pt8 Solve word problems involving calculations with whole numbers, fractions, percentages, decimals, money or measures, including multi-step problems


## Using understanding and strategies in solving problems

- 8Ps1 Identify the mathematical features of a context or problem; try out and compare mathematical representations using accurate notation
- 8Ps2 Conjecture and generalise, identifying exceptional cases or counter-examples
- 8Ps3 Use logical argument to interpret the mathematics in a context or to establish the truth of a statement
- 8Ps4 Give accurate solutions appropriate to the context or problem
- 8Ps5 Record and compare reasoning, solutions and conclusions
- 8Ps6 Refine approaches and findings on the basis of discussions with others


## Stage 9

## Number

## Ni Integers, powers and roots

- 9Ni1 Add, subtract, multiply and divide directed numbers
- 9 Ni 2 Estimate square roots and cube roots
- $\mathbf{9 N i 3}$ Use positive, negative and zero indices and the index laws for multiplication and division of positive integer powers

Np Place value, ordering and rounding

- $\quad 9 \mathrm{~Np} 1$ Recognise the equivalence of $0.1, \frac{1}{10}$ and $10^{-1}$; multiply and divide whole numbers and decimals by 10 to the power of any positive or negative integer
- $\mathbf{9 N p 2}$ Round numbers to a given number of decimal places or significant figures; use to give solutions to problems with an appropriate degree of accuracy
- $\quad \mathbf{9 N p} 3$ Use the order of operations, including brackets and powers

Nf Fractions, decimals, percentages, ratio and proportion

- 9Nf1 Consolidate writing a fraction in its simplest form by cancelling common factors
- $9 N f 2$ Add, subtract, multiply and divide fractions, interpreting division as a multiplicative inverse, and cancelling common factors before multiplying or dividing
- $9 N f 3$ Solve problems involving percentage changes, choosing the correct numbers to take as $100 \%$ or as a whole, including simple problems involving personal or household finance, e.g. simple interest, discount, profit, loss and tax
- 9Nf4 Recognise when fractions or percentages are needed to compare different quantities
- $9 N f 5$ Compare two ratios; interpret and use ratio in a range of contexts
- 9Nf6 Recognise when two quantities are directly proportional; solve problems involving proportionality, e.g. converting between different currencies


## Nc Calculation

## Mental strategies

- 9Nc1 Extend mental methods of calculation, working with decimals, fractions, percentages and factors, using jottings where appropriate
- 9Nc2 Solve word problems mentally
- $\mathbf{9 N c 3}$ Consolidate use of the rules of arithmetic and inverse operations to simplify calculations


## Multiplication and division

- 9Nc4 Multiply by decimals, understanding where to position the decimal point by considering equivalent calculations; divide by decimals by transforming to division by an integer
- 9Nc5 Recognise the effects of multiplying and dividing by numbers between 0 and 1


## Algebra

## Ae Expressions, equations and formulae

- 9Ae1 Know the origins of the word algebra and its links to the work of the Arab mathematician Al'Khwarizmi
- 9Ae2 Use index notation for positive integer powers; apply the index laws for multiplication and division to simple algebraic expressions
- 9Ae3 Construct algebraic expressions
- 9Ae4 Simplify or transform algebraic expressions by taking out single-term common factors
- 9Ae5 Add and subtract simple algebraic fractions
- 9Ae6 Derive formulae and, in simple cases, change the subject; use formulae from mathematics and other subjects
- 9Ae7 Substitute positive and negative numbers into expressions and formulae
- 9Ae8 Construct and solve linear equations with integer coefficients (with and without brackets, negative signs anywhere in the equation, positive or negative solution); solve a number problem by constructing and solving a linear equation
- 9Ae9 Solve a simple pair of simultaneous linear equations by eliminating one variable
- 9Ae10 Expand the product of two linear expressions of the form $x \pm n$ and simplify the corresponding quadratic expression
- 9Ae11 Understand and use inequality signs $(<\rangle,, \leqslant, \geqslant)$; construct and solve linear inequalities in one variable; represent the solution set on a number line

As Sequences, functions and graphs

- 9As1 Generate terms of a sequence using term-to-term and position-to-term rules
- 9As2 Derive an expression to describe the $n$th term of an arithmetic sequence
- 9As3 Find the inverse of a linear function
- 9As4 Construct tables of values and plot the graphs of linear functions, where $y$ is given implicitly in terms of $x$, rearranging the equation into the form $y=m x+c$; know the significance of $m$ and find the gradient of a straight line graph
- 9As5 Find the approximate solutions of a simple pair of simultaneous linear equations by finding the point of intersection of their graphs
- 9As6 Use systematic trial and improvement methods to find approximate solutions of equations such as $x^{2}+2 x=20(1,2$ and 7$)$
- 9As7 Construct functions arising from real-life problems; draw and interpret their graphs
- 9As8 Use algebraic methods to solve problems involving direct proportion, relating solutions to graphs of the equations


## Geometry

## Gs Shapes and geometric reasoning

- 9Gs1 Calculate the interior or exterior angle of any regular polygon; prove and use the formula for the sum of the interior angles of any polygon; prove that the sum of the exterior angles of any polygon is $360^{\circ}$
- 9Gs2 Solve problems using properties of angles, of parallel and intersecting lines, and of triangles, other polygons and circles, justifying inferences and explaining reasoning with diagrams and text
- 9Gs3 Draw 3D shapes on isometric paper
- 9Gs4 Analyse 3D shapes through plans and elevations
- 9Gs5 Identify reflection symmetry in 3D shapes
- 9Gs6 Use a straight edge and compasses to:
- construct the perpendicular from a point to a line and the perpendicular from a point on a line
- inscribe squares, equilateral triangles, and regular hexagons and octagons by constructing equal divisions of a circle
- 9Gs7 Know and use Pythagoras' theorem to solve two-dimensional problems involving right-angled triangles


## Gp Position and movement

- 9Gp1 Tessellate triangles and quadrilaterals and relate to angle sums and half-turn rotations; know which regular polygons tessellate, and explain why others will not
- 9Gp2 Use the coordinate grid to solve problems involving translations, rotations, reflections and enlargements
- 9Gp3 Transform 2D shapes by combinations of rotations, reflections and translations; describe the transformation that maps an object onto its image
- 9Gp4 Enlarge 2D shapes, given a centre and positive integer scale factor; identify the scale factor of an enlargement as the ratio of the lengths of any two corresponding line segments
- 9Gp5 Recognise that translations, rotations and reflections preserve length and angle, and map objects on to congruent images, and that enlargements preserve angle but not length
- 9Gp6 Know what is needed to give a precise description of a reflection, rotation, translation or enlargement
- 9Gp7 Use bearings (angles measured clockwise from the north) to solve problems involving distance and direction
- 9Gp8 Make and use scale drawings and interpret maps
- 9Gp9 Find by reasoning the locus of a point that moves at a given distance from a fixed point, or at a given distance from a fixed straight line


## Measure

Gl Length, mass and capacity
9Gl1

- 9M11 Solve problems involving measurements in a variety of contexts

Gt Time and rates of change
9Gt1 - 9Mt1 Solve problems involving average speed
9Gt2 - 9Mt2 Use compound measures to make comparisons in real-life contexts, e.g. travel graphs and value for money

## Ga Area, perimeter and volume

9Ga1 - 9Ma1 Convert between metric units of area, e.g. $\mathrm{mm}^{2}$ and $\mathrm{cm}^{2}, \mathrm{~cm}^{2}$ and $\mathrm{m}^{2}$ and volume, e.g. $\mathrm{mm}^{3}$ and $\mathrm{cm}^{3}, \mathrm{~cm}^{3}$ and $\mathrm{m}^{3}$; know and use the relationship $1 \mathrm{~cm}^{3}=1 \mathrm{ml}$
9Ga2 - 9Ma2 Know that land area is measured in hectares (ha), and that 1 hectare $=10000 \mathrm{~m}^{2}$; convert between hectares and square metres
9Ga3 - 9Ma3 Solve problems involving the circumference and area of circles, including by using the $\pi$ key of a calculator

9Ga4 - 9Ma4 Calculate lengths, surface areas and volumes in right-angled prisms and cylinders

## Handling data

## Dc Planning and collecting data

- 9Dc1 Suggest a question to explore using statistical methods; identify the sets of data needed, how to collect them, sample sizes and degree of accuracy
- 9Dc2 Identify primary or secondary sources of suitable data
- 9Dc3 Design, trial and refine data collection sheets
- 9Dc4 Collect and tabulate discrete and continuous data, choosing suitable equal class intervals where appropriate


## Dp Processing and presenting data

- 9Dp1 Calculate statistics and select those most appropriate to the problem
- 9Dp2 Select, draw, and interpret diagrams and graphs, including:
- frequency diagrams for discrete and continuous data
- line graphs for time series
- scatter graphs to develop understanding of correlation
- back to back stem-and-leaf diagrams


## Di Interpreting and discussing results

- 9Di1 Interpret tables, graphs and diagrams and make inferences to support or cast doubt on initial conjectures; have a basic understanding of correlation
- 9Di2 Compare two or more distributions; make inferences, using the shape of the distributions and appropriate statistics
- 9Di3 Relate results and conclusions to the original question


## Db Probability

- 9Db1 Know that the sum of probabilities of all mutually exclusive outcomes is 1 and use this when solving probability problems
- 9Db2 Find and record all outcomes for two successive events in a sample space diagram
- 9Db3 Understand relative frequency as an estimate of probability and use this to compare outcomes of experiments in a range of contexts


## Problem solving

## Using techniques and skills in solving mathematical problems

- 9Pt1 Calculate accurately, choosing operations and mental or written methods appropriate to the numbers and context
- 9Pt2 Manipulate numbers, algebraic expressions and equations, and apply routine algorithms
- 9Pt3 Understand everyday systems of measurement and use them to estimate, measure and calculate
- 9Pt4 Recognise and use spatial relationships in two dimensions and three dimensions
- 9Pt5 Draw accurate mathematical diagrams, graphs and constructions
- 9Pt6 Decide how to check results, by:
- using rounding to estimate numbers to one significant figure and calculating mentally then comparing with the estimate
- considering whether an answer is reasonable in the context of the problem
- using inverse operations
- 9Pt7 Estimate, approximate and check their working. Solve a range of word problems involving single or multistep calculations


## Using understanding and strategies in solving problems

- 9Ps1 Identify, organise, represent and interpret information accurately in written, tabular, graphical and diagrammatic forms
- 9Ps2 Explore the effect of varying values in order to generalise
- 9Ps3 Find a counter-example to show that a conjecture is not true
- 9Ps4 Present concise, reasoned arguments to justify solutions or generalisations using symbols, diagrams or graphs and related explanations
- 9Ps5 Recognise the impact of constraints or assumptions
- 9Ps6 Recognise connections with similar situations and outcomes
- 9Ps7 Consider and evaluate the efficiency of alternative strategies and approaches and refine solutions in the light of these

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